

**The Islamic University Of Gaza**  
**Department of Mathematics**  
**Calculus A (MathA1401) summer semester**

**Date: 21/8/2007**

**Final Exam**

**Time: 2 Hour**

St. Name	Q1	Q2	Q3	Q4	Q5	Q6	Q7	Total
St. no.	10	15	16	16	12	16	15	100
Instructor Dr.Mohammed M. Al-Ashker								

**Answer all the following questions:**

Q.1) Circle the corrected answer for each of the following:-

- (1) If  $\int_2^4 f(x)dx = \frac{1}{4}$  and  $\int_2^4 g(x)dx = 5$ . Then  $\int_2^4 (5f(x) - \frac{1}{3}g(x))dx =$   
 (a)  $\frac{15}{12}$       (b)  $\frac{10}{12}$       (c)  $\frac{-5}{12}$       (d)  $\frac{20}{12}$ .
- (2) The graph of the function  $y = \frac{10x+3}{2x-5}$  has a horizontal asymptote at:  
 (a)  $y = 5$       (b)  $y = \frac{3}{5}$       (c)  $y = \frac{-3}{5}$       (d)  $y = -5$ .
- (3)  $\lim_{x \rightarrow 6} 7 =$   
 (a) 1      (b) -1      (c) 7      (d) dos't exist.
- (4) If  $\lim_{x \rightarrow 3} \frac{x}{x-3} =$   
 (a) 0      (b)  $-\infty$       (c)  $\infty$       (d) dos't exist.
- (5) The equation of the tangent line to the curve  $y = 2x$  at  $x = 3$  is:  
 (a)  $y = 2x$       (b)  $y = 2x - 3$       (c)  $y = 2x + 3$       (d)  $y = 2$ .
- (6)  $\frac{d^{71}(\sin x)}{dx^{71}} =$   
 (a)  $-\cos x$       (b)  $\sin x$       (c)  $\cos x$       (d)  $-\sin x$ .
- (7) The function  $f(x) = \frac{1}{x}$  has an absolute maximum on the interval  $[1, 3]$  of:  
 (a) 1      (b) 9      (c)  $\frac{1}{3}$       (d)  $\frac{1}{9}$ .
- (8) Where is the function  $y = \cos x$  increasing on the interval  $[0, 2\pi]$ ?  
 (a)  $[0, \pi]$       (b)  $[\pi, 2\pi]$       (c)  $[\frac{\pi}{2}, \frac{3\pi}{2}]$       (d)  $[0, \frac{\pi}{2}] \cup [\frac{3\pi}{2}, 2\pi]$ .
- (9) The average value of the function  $f(x) = \sqrt{4-x^2}$  on the closed interval  $[-2, 2]$  equals:  
 (a)  $\pi$       (b)  $\frac{\pi}{2}$       (c)  $2\pi$       (d)  $\frac{\pi}{4}$ .
- (10)  $\lim_{x \rightarrow 0} \frac{1 - \cos x}{\sin x} =$   
 (a) 0      (b) 1      (c) does not exist      (d)  $\infty$ .

Q.2) (a) For the limit  $\lim_{x \rightarrow -3} \sqrt{1 - 5x} = 4$ . Find a  $\delta > 0$  that works for  $\varepsilon = 0.5$ .

(b) Let  $x^2 + 2xy + y^4 = 1$ . Find  $\frac{dy}{dx}$ .

(c) Let  $f(x) = \sqrt{2x + 1}$ . Use the limit definition of derivative to find  $f'(x)$ .

Q.3) Let  $f(x) = -x^3 - 3x^2 + 9x + 13$ .

(a) Find critical points of  $f(x)$ .

(b) On what intervals is  $f(x)$  increasing and decreasing?, determine local maximum and local minimum values of  $f(x)$ .

(c) On what intervals is the graph of  $f(x)$  is concave up? concave down?. Find the points of inflection of  $f(x)$ .

(d) Sketch the graph of  $f(x)$ .

Q.4) Find the following limits.

(a)  $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2 - 1}}{2x + 1}.$

(b)  $\lim_{x \rightarrow 0} \frac{\tan 5x}{3x}.$

(c)  $\lim_{x \rightarrow 1^+} \frac{x^2 - 1}{(x - 1)^2}.$

(d)  $\lim_{x \rightarrow \infty} x - \sqrt{x^2 - 2x + 5}.$

Q.5) Find  $f'(x)$  for the following functions.

(a)  $f(x) = (x^4 + \sqrt{x} + 1)^{\frac{1}{4}}.$

(b)  $f(x) = \sec 2x + \frac{\sin 2x + \cos x}{1+x^2}.$

(c)  $f(x) = \int_{x^2}^{x^3} (1 + \sin t^2) dt.$

Q.6) Evaluate the following integrals:

(a)  $\int x^2 + \frac{2}{x^{\frac{5}{2}}} dx.$

(b)  $\int x\sqrt{x-1} dx.$

(c)  $\int \frac{\sin\sqrt{x}}{\sqrt{x}} dx.$

(d)  $\int_{-2}^3 |x+1| dx.$

Q.7) (a) Find the area of the region bounded by the curves  $x = y^2$  and  $x - 2y = 3$ .

(b) The region in the first quadrant bounded by  $y = x^2 + 1$  and  $y = 2$  is revolved about the line  $y = 1$  to generate a solid, find the volume of the solid.